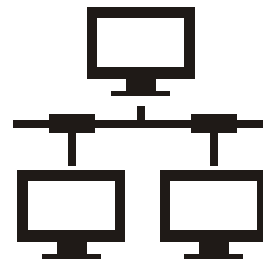


COMPUTER SCIENCE & IT



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Grammars, Languages & Automata

Multiple Choice Questions & NAT Questions

- Q.1** Suppose $L_1 = \{10, 1\}$ and $L_2 = \{011, 11\}$. How many distinct elements are there in $L = L_1 L_2$.
 (a) 4 (b) 3
 (c) 2 (d) None of these
- Q.2** In a string of length n , how many proper prefixes can be generated
 (a) 2^n (b) n
 (c) $\frac{n(n+1)}{2}$ (d) $n-1$
- Q.3** Let $u, v, \in \Sigma^*$ where $\Sigma = \{0, 1\}$. Which of the following are TRUE?
 1. $|u.v| = |v.u|$
 2. $u.v = v.u$
 3. $|u.v| = |u| + |v|$
 4. $|u.v| = |u| |v|$
 (a) 1 and 3 (b) 1, 2 and 3
 (c) 2 and 4 (d) 1, 2 and 4
- Q.4** How many odd palindromes of length 11 are possible with alphabet $S = \{a, b, c\}$
 (a) 3^6 (b) 2^5
 (c) 2^6 (d) 3^5
- Q.5** The number of distinct subwords present in 'MADEEASY' are _____.
- Q.6** Consider the following statements:
 1. Type 0 grammars generate all languages which can be accepted by a Turing machine.
 2. Type 1 grammars generate the languages which can all be recognized by a push down automata.
 3. Type 3 grammars have one to one correspondence with the set of all regular expressions.
 4. There are some languages which are not accepted by a Turing machine.
 Which of the above statements are TRUE?
 (a) 1, 2 and 3 (b) 1, 2 and 4
 (c) 1, 3 and 4 (d) 2, 3 and 4

- Q.7** Consider the following table of an FA:

δ	a	b
start	q_1	q_0
q_0	q_1	q_0
q_1	q_2	q_1
q_2	q_3	q_2
q_3	q_4	q_3
q_4	q_4	q_4

If the final state is q_4 , the which of the following strings will be accepted?

- aaaaa
 - aabbaabbbb
 - bbabababbb
- (a) 1 and 2 (b) 2 and 3
 (c) 3 and 1 (d) All of these

- Q.8** Which of the following statements is correct?
 (a) Some finite automata accept non regular languages.
 (b) A grammar with recursion always generates infinite languages.
 (c) An infinite language can be generated by a non recursive grammar.
 (d) A deterministic push down automata cannot generate all context free languages.
- Q.9** The grammar with start symbol S over $\Sigma = \{a, b\}$ $S \rightarrow aSbb \mid abb$ belongs to the class
 (a) Type 0 (b) Type 1
 (c) Type 2 (d) Type 3
- Q.10** What is the language generated by the grammar where S is the start symbol and the set of terminals and non terminals is $\{a\}$ and $\{A, B\}$ respectively?
 $S \rightarrow Aa$
 $A \rightarrow B$
 $B \rightarrow Aa$
 (a) Set of strings with atleast one a
 (b) Set of strings with even number of a 's
 (c) Set of strings with odd number of a 's
 (d) Empty language

Q.11 How many even palindromes of length atmost 10 are possible with alphabet $\Sigma = \{0, 1, 2\}$?

- (a) $\frac{3^5 - 1}{2}$ (b) $3^5 - 1$
(c) $\frac{3^6 - 1}{2}$ (d) $3^6 - 1$

Q.12 Consider the languages $L_1 = \phi$ and $L_2 = \{1\}$. Which one of the following represents $L_1^* \cup L_2^* L_1^*$?

- (a) $\{\lambda\}$ (b) $\{\lambda, 1\}$
(c) ϕ (d) 1^*

Q.13 Given language, $L_1 = \{a^n b^n\}$ and $L_2 = \{a^{2n} b^{2n}\}$. Identify the statements which are TRUE.

1. The language obtained by intersection of languages L_1 and L_2 is same as L_2 .
2. The language obtained by performing $L_1 - L_2$ is given by $L_3 = \{a^{2n+1} b^{2n+1}\}$
3. The language obtained by union of L_1 and L_2 is same as L_1 .
4. The language obtained by performing $L_2 - L_1$ is empty.

Which of the above statements are correct?

- (a) 1, 2 and 3 (b) 1 and 3
(c) 3 and 4 (d) All are correct

Q.14 Let, $L_1 = \{a^n b^n c^n \mid n \geq 0\}$
 $L_2 = \{a^{2n} b^{2n} c^{2n} \mid n \geq 0\}$
 $L_3 = \{a^{2n} b^{2n} c^n \mid n \geq 0\}$

- (a) $L_1 \subseteq L_2$ and $L_3 \subseteq L_2$
(b) $L_2 \subseteq L_1$ and $L_2 \subseteq L_3$
(c) $L_2 \subseteq L_1$ but $L_2 \not\subseteq L_3$
(d) $L_1 \subseteq L_2$ and $L_2 \subseteq L_3$

Q.15 Let $L = \{ab, aa, baa\}$. How many of the following strings are in L^* ?

- (a) abaabaaabaa (b) baaaaabaa
(c) baaaaabaaaab (d) aaaabaaaa

Q.16 The prefix of a language is defined as prefix $(L) = \{x : xy \in L \text{ for some } y \in \Sigma^*\}$ and the suffix is defined as suffix $(L) = \{y : xy \in L \text{ for some } x \in \Sigma^*\}$. Which of the following statements is always correct?

- (a) $\text{prefix}(L) \cap \text{suffix}(L) = \phi$
(b) $\text{prefix}(L) \cap \text{suffix}(L) \supseteq (\Sigma, L)$
(c) $\text{prefix}(L) \cap \text{suffix}(L) \subseteq (\Sigma, L)$
(d) $\text{prefix}(L) \cap \text{suffix}(L) = (\Sigma, L)$

Q.17 Let, $L_1 =$ (Strings with any number of a 's followed by any number of b 's) and $L_2 = (ba)$. $L_3 =$ Prefix $(L_1^* \cap L_2)$. The number of strings in L_3 will be _____.

Q.18 What language does the grammar with these productions generate?

$S \rightarrow aaA$

$A \rightarrow aA \mid \epsilon$

- (a) strings with even number of a 's
(b) strings with odd number of a 's
(c) strings with atmost 2 a 's
(d) strings with atmost 2 a 's

Q.19 Let, $L_1 = \{a^* b^*\}$ and $L_2 = \{b^* a^*\}$. The language $L = L_1 \cap L_2$ is represented by

- (a) ϕ (b) $a^* + b^*$
(c) $a^* b^*$ (d) $(a + b)^*$

Q.20 Let $L_1 = \{a^n \mid n \geq 0\}$ and $L_2 = \{b^n \mid n \geq 0\}$. Then L is given by $L_1 L_2$. Which of the following statement(s) is/are true about L ?

1. L is the language of strings with equal number of a 's followed by an equal number of b 's.
 2. L is a context free language but not regular.
 3. L is regular.
 4. $L = \{a^n b^n \mid n \geq 0\}$
- (a) 1, 2 and 4 (b) 1, 3 and 4
(c) 1 and 4 (d) 3 only

Q.21 How many of the following statements are correct?

1. Both L and \bar{L} can be finite
 2. $(\bar{L}^*) = (\bar{L})^*$
 3. $(L_1 L_2)^R = (L_2)^R (L_1)^R$
 4. $(L^*)^* = L^*$
- (a) Only 1 (b) Only 2
(c) 1 and 2 (d) All of the above

Q.22 Given $L = \{a^n \mid n \geq 0\}$ over $\Sigma = \{a\}$. What is the language represented by L^2 ?

- (a) Set of all strings over Σ with odd length
(b) Set of all strings over Σ with even length
(c) Set of all strings over Σ
(d) None of these

Q.23 Let, $L = \{\lambda, 0, 01, 10\}$. Which of the following strings does not belong to L^5 ?

- (a) 110010 (b) 101001001
(c) 100100 (d) 01101001

Q.24 Which of the following conversions is not possible?

- (a) Regular grammar to context free grammar
- (b) NFA to DFA
- (c) Non deterministic PDA to deterministic PDA
- (d) Non deterministic Turing machine to deterministic Turing machine

Q.25 If $S = \{ab, ba\}$, which of the following is true?

- (a) S^* contains finite no of strings of infinite length.
- (b) S^* has no strings having 'aaa' or 'bbb' as substring.
- (c) S^* has no strings having aa as substring.
- (d) If $T = \{a, b\}$, then $S^* \not\subseteq T^*$,

Multiple Select Questions (MSQ)

26. Given the language $L = \{ab, aa, baa\}$, which of the following strings are in L^* ?

- (a) abaabaaabaa
- (b) aaaabaaaa
- (c) baaaaabaaaab
- (d) baaaaabaa

■■■■

Answers Grammars, Languages & Automata

- | | | | | | | | | |
|---------|---------|---------|---------|---------|---------|---------|---------------|---------|
| 1. (b) | 2. (b) | 3. (a) | 4. (a) | 5. (34) | 6. (c) | 7. (a) | 8. (d) | 9. (c) |
| 10. (d) | 11. (c) | 12. (d) | 13. (d) | 14. (c) | 15. (c) | 16. (b) | 17. (3) | 18. (d) |
| 19. (b) | 20. (d) | 21. (b) | 22. (c) | 23. (a) | 24. (c) | 25. (b) | 26. (a, b, d) | |

Explanations Grammars, Languages & Automata

1. (b)

$$L_1 = \{10, 1\},$$

$$L_2 = \{011, 11\}$$

By concatenation of L_1 and L_2 we get

$$L_1 \cdot L_2 = \{10011, 1011, 1011, 111\}$$

Hence, 3 distinct elements are there.

2. (b)

Suppose, $S = aaab$, $|s| = 4$. The prefixes are $S_p = \{\lambda, a, aa, aaa, aaab\}$. Here aaab is not a proper prefix.

Note: The proper prefix of string S is a prefix, which is not same as string S .

A string of length 4 has 4 proper prefixes. A string of length 5 has 5 proper prefixes. For a string of length n , therefore we can have ' n ' proper prefixes.

3. (a)

Let, $u = 1001$ and $v = 001$
 $u.v = 1001001$ and $v.u = 0011001$
 $|u, v| = |v, u| = |u| + |v|$
 But $u.v \neq v.u$

4. (a)

Palindromes can be represented by $\{WW^R \mid W \in \{a, b, c\}^*\}$

$$\{WxW^R \mid W \in \{a, b, c\}^*, x \in \{a, b, c\}\}$$

Since, we need to count the number of odd palindromes of length 11, the number of possible W 's of length 5 are $|\Sigma|^5$ i.e. 3^5

Number of possible ways for $x = 3$

$$\therefore \text{Number of odd palindromes of length 11} = 3^5 \times 3 = 3^6$$

Number of odd palindromes of length,

$$n = \left\lceil \frac{n-1}{2} \right\rceil \times |\Sigma| = \left\lceil \frac{n+1}{2} \right\rceil$$

5. (34)

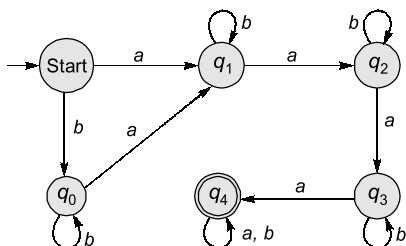
Distinct subwords of

- | | |
|--------------|--------------|
| Length 1 = 6 | Length 5 = 4 |
| Length 2 = 7 | Length 6 = 3 |
| Length 3 = 6 | Length 7 = 2 |
| Length 4 = 5 | Length 8 = 1 |

$$\therefore \text{Total} = 34$$

6. (c)

See Chomsky Hierarchy languages, which are not recursively enumerable are not recognized by any machine.

7. (a)

Drawing the FA we have we can clearly see that only (i) *aaaaa* and (ii) *aabbaabbbbbb* are accepted.

8. (d)

- (a) Is false since a FA can accept only regular languages as it has finite memory only.
- (b) Is false consider the grammar $\{S \rightarrow Sa\}$ which is recursive. It generates the empty language i.e. \emptyset which is finite.
- (c) Is false. To generate an infinite language, the grammar must have recursion.
- (d) True DPDA cannot generate all CFLs. It generates a subset of CFLs called DCFLs. DPDA has less recognition power than a PDA.

9. (c)

The given grammar is Type 2 as every rule is restricted as:

$$V \rightarrow (VUT)^*$$

where V is the set of non-terminals and T is set of terminals.

10. (d)

Since there is no string which can be generated from the grammar in finite number of steps as there is no termination, (d) is true.

11. (c)

If the sequence has even length say, $n = 2k$, selecting the first k characters completely determines the palindrome since the remaining k characters can be found by repeating the sequence

in the reverse order. Number of palindromes of even length at most n in alphabet with x characters is

$$x^0 + x^1 + x^2 + \dots + x^k = \frac{-1 + x^{k+1}}{x - 1}.$$

Here, $x = 3$ and $k = 5$

$\therefore \frac{3^6 - 1}{2}$ is the number of palindromes of length at most 10.

12. (d)

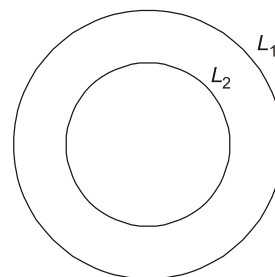
$$L_1^* = \{\emptyset\}^* = \{\lambda\}$$

$$L_2^* = \{1\}^* = 1^*$$

$$L_1^* \cup L_2^* = \{\lambda\} \cup \{1\}^* = 1^*$$

13. (d)

L_1 is the set of all strings where any number of a 's is followed by an equal number of b 's.



L_2 is the set of all strings where an even number of a 's is followed by an equal number of b 's.

$$\therefore L_2 \subseteq L_1$$

$$L_2 \cap L_1 = L_2$$

$$L_2 \cup L_1 = L_1$$

$L_1 - L_2 =$ (Set of all strings where an odd number of a 's is followed by an equal number of b 's)

$$L_2 - L_1 = \emptyset$$

14. (c)

$$L_1 = \{a^n b^n c^n, n \geq 0\} \\ = \{\lambda, abc, a^2b^2c^2, \dots\}$$

$$L_2 = \{a^{2n} b^{2n} c^{2n}, n \geq 0\} \\ = \{\lambda, a^2b^2c^2, a^4b^4c^4, \dots\}$$

$$L_3 = \{a^{2n} b^{2n} c^n, n \geq 0\} \\ = \{\lambda, a^2b^2c, a^4b^4c^2, \dots\}$$

as we can easily see that

- (i) L_1 contains all the words generated by L_2 and also it contains some extra strings.