

# CIVIL ENGINEERING

CONVENTIONAL Practice Sets

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## **Water Demand**

Q.1 The present population of a community is 28000 with an average water consumption of 4200 m<sup>3</sup>/d. The existing water treatment plant has a design capacity of 6000 m<sup>3</sup>/d. It is expected that the population will increase to 44000 during the next 20 years. Find the number of years from now when the plant will reach its design capacity, assuming an arithmetic rate of population growth

#### **Solution:**

**Given dat:** Present population,  $P_0 = 28000$ ; Population after 20 years,  $P_n = 44000$ 

 $\therefore$  Increase in population per year,  $\bar{x}$ 

$$\overline{x} = \frac{P_n - P_0}{n}$$

$$= \frac{44000 - 28000}{20} = 800$$

Now, for population for 28000, water consumption = 4200 m<sup>3</sup>/d Hence, population for water consumption of 6000 m<sup>3</sup>/d

$$= \frac{28000}{4200} \times 6000 = 40000 \text{ persons} = \text{Population at design capacity}$$

: No. of years from now when plant will reach at design capacity

$$P_n = P_0 + n\overline{x}$$

$$n = \frac{40000 - 28000}{800} = 15 \text{ years}$$

What is meant by 'design period' and 'population forecast'? Describe the 'incremental increase' method of future population forecast of a city, stating its advantages.

#### **Solution:**

Design Period: The number of years for which the system is to be adequate is called design period.

**Population forecasting:** Design of water supply and sanitation scheme is based on the projected population of a particular city, estimated for the design period. Any underestimated value will make system inadequate for the purpose intended, similarly overestimated value will make it costly.

The present and past population record for the city can be obtained for the census population record. After collecting these population figures, the population at the end of design period is predicted using various methods as suitable for that city considering the growth pattern followed by the city.

**Incremental Increase method:** This method is modification of arithmetical increase method and it is suitable for an average size town under normal condition where the growth rate is found to be in increasing order. While adopting this method, the increase in increment is considered for calculating future population. The incremental increase is determined for each decade from the past population and the average value is added to the present population along with the average rate of increase.



Hence, population after  $n^{th}$  decade is  $P_n = P + nX + \left\{ \frac{(n+1)n}{2} \right\} Y$ 

Where,  $P_n = \text{Population after } n^{\text{th}} \text{ decade}$ 

X = Average increaseY = Incremental increase

- Advantages of incremental increase method:
  - 1. This method gives/predict more accurate value of population.
  - 2. This method embodies the advantage of arithmetic average method and geometrical average method.

Q3 The population of a city at previous consecutive census year was 4,00,000, 5,58,500, 7,76,000 and 10,98,500. Calculate the anticipated population at the next census nearest to 5,000

#### **Solution:**

Since the method is not mentioned in the question, hence the question is solved by *incremental increase method*. This is done because

- This method gives results between the results given by the arithmetic increase method and the geometric increase method.
- The method is considered to be the best for any city, whether old or new.

Census year	Population	Population Increment	Incremented Increase
1 2 3 4	4,00,000 5,58,500 7,76,000 10,98,500	- 1,58,500 - 2,17,500 - 3,22,500	— 59000 —10,5000
		$\overline{X} = \frac{\Sigma X}{3}$ $= 232833.33$	$\overline{Y} = \frac{\Sigma Y}{2}$ $= 82000$

$$P_n = P_0 + n \cdot \overline{X} + \frac{n(n+1)}{2} \overline{Y}$$

For

$$P_5 = P_0 + 1 \cdot \overline{X} + \frac{1(1+1)}{2} \overline{Y}$$

$$= 10,98,500 + 232833.33 + 82000 = 1413333.33$$

- .. The anticipated population at the next census to the nearest 5000 would be 1415000.
- Q4 Compute the 'fire demand' for a city of 2 lac population by any two formulae including that of the National Board of Fire Underwriters.

#### **Solution:**

(i) The rate of fire demand as per **National Board of Fire Underwriters formula** for a central congested city whose population is less than or equal to 2 lakh is given by

$$Q = 4637\sqrt{P}(1 - 0.01\sqrt{P})$$

where Q is amount of water required in litres per minute and P is population in thousands

$$Q = 4637\sqrt{200} \left[ 1 - 0.01\sqrt{200} \right] = 56303.08 \text{ litres per minute}$$
$$= \frac{56303.08 \times 60 \times 24}{10^6} \text{MLD} = 81.08 \text{ MLD}$$

(ii) Kuichling's formula,

$$Q = 3182\sqrt{P} = 3182\sqrt{200}$$
  
= 45000.28 litres per minute = 64.8 MLD





(iii) Freeman Formula,

$$Q = 1136 \left[ \frac{P}{10} + 10 \right]$$
= 1136 \left[ \frac{200}{10} + 10 \right] = 34080 \text{ litres per minute} = 49.0752 \text{ MLD}

(iv) Buston's formula,

$$Q = 5663\sqrt{P} = 5663\sqrt{200}$$
  
= 80086.91 litres per minute = 115.33 MLD

Q5 Explain any three methods of estimating the future population of a city. What are their relative merits?

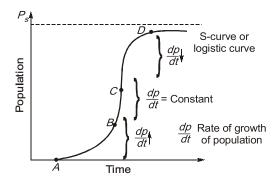
#### **Solution:**

Population forecasting: General population growth curve with respect to time is given by following method:

 Arithmetic increase method: In this method rate of growth of population is assumed to be constant

i.e. for region BC. for which 
$$\frac{dp}{dt}$$
 = Constant, i.e., population increases by same amount in a given time duration.

2. Geometric increase method (compound/uniform increase method): In this method rate of growth of population is assumed constant but population is compounded for this given rate to compute population in future.



- **3.** Incremental increase method: In this method, rate of growth of population is not assumed to be constant. Rate of growth of population may increase or decrease. In this method average incremental increase in increase of population is also considered.
- 4. Merits of different forecasting methods:
  - (a) Population forecasted by geometric increase method is maximum in comparison to that computed by arithmetic or increment increase method.
  - (b) Population forecasted with arithmetic increase method is minimum in comparison to geometric increase method and incremental increase method.
  - (c) Geometric increase method is generally recommended for young cities and arithmetic increase method for old ones.

Q.6 Compute the population of the year 2000 and 2006 for a city whose population in the year 1930 was 25000 and in year 1970 was 47000. Make use of geometric increase method.

#### **Solution:**

The growth rate can be computed by,

$$r = \sqrt[n]{\frac{P_2}{P_1}} - 1 = \sqrt[4]{\frac{47000}{25000}} - 1 = 0.17095$$
  
= 17.095% per decade

Now, using  $P_n = P_0 \left( 1 + \frac{r}{100} \right)^n$ , we have



$$P_{2000} = P_3$$
 (i.e., after 3 decades from 1970 onwards)  

$$= P_{1970} \left( 1 + \frac{r}{100} \right)^3 = 47000(1 + 0.17095)^3 = 75459$$
 $P_{2006} = P_{3.6}$ 

$$= P_{1970} (1 + 0.17095)^{3.6} = 47000 (1 + 0.17095)^{3.6}$$

$$= 82954$$

and

Q.7 A city has following recorded population:

<b>1951</b> 50000	
1971	110000
1991	160000

Estimate: (i) the saturation population, and (ii) expected population in 2011. (Use Logistic Curve Method)

#### **Solution:**

*:*:.

**Given data:** n = 20 years,  $P_0 = 50000$ ,  $P_1 = 110000$ ,  $P_2 = 160000$ 

Saturation population, 
$$P_S = \frac{2P_0P_1P_2 - P_1^2(P_0 + P_2)}{P_0P_2 - P_1^2}$$

$$P_{S} = \frac{2 \times 50000 \times 110000 \times 160000 - (110000)^{2} (50000 + 160000)}{50000 \times 160000 - (110000)^{2}}$$

$$\simeq 190488$$

$$P_{t} = \frac{P_{s}}{1 + \left(\frac{P_{s} - P_{o}}{P_{o}}\right)} e^{(-kP_{s}t)} = \frac{P_{s}}{1 + \left(\frac{P_{s} - P_{o}}{P_{o}}\right)} e^{nt}$$
(where  $n = -kP_{s}$ )

$$n = \frac{1}{t_1} \ln \left[ \frac{P_o(P_s - P_1)}{P_1(P_s - P_o)} \right] = \frac{1}{20} \ln \left[ \frac{50000(190488 - 110000)}{11000(190488 - 50000)} \right] = -0.0673$$

$$P = \frac{190488}{1 + 2.80976 \times e^{-0.0673 \times 60}} = 181496$$

Q.8 The population of a town as per the census records are given below for the years 1921 to 1981. Assuming that the scheme of water supply will commence to function from 1986, it is required to estimate the population 30 years hence, i.e., in 2016 and also the intermediate population 15 years after 1986, i.e., 2001. Using arithmetic increase method, geometric increase method and incremental increase method, estimate the population in 2001 and 2016.

Year	Population
1921	40,185
1931	44,522
1941	60,395
1951	75,614
1961	98,886
1971	124,230
1981	158,800





#### **Solution:**

Year	Population	Increment
1921	40,185	_
1931	44,522	4,337
1941	60,395	15,873
1951	75,614	15,219
1961	98,886	23,272
1971	124,230	25,344
1981	158,800	34,570
	118,615	
	19,769	

#### 1. Arithmetical Progression Method

Increase in population from 1921 to 1981

i.e., in 6 decades = 158800 - 40185 = 118615

or, increase per decade  $= \frac{1}{6} \times 118615 = 19769$ 

Population in 2001 = Population in 1981 + Increase for 2 decades

= 158800 + 2 × 19769 = 158800 + 39538 = 198338

Population in 2016 = Population in 1981 + Increase for 3.5 decades

 $= 158800 + 3.5 \times 19769 = 227992$ 

#### 2. Geometrical Progression Method

Rate of growth from 1931 to 1941 =  $\frac{4337}{40185}$  = 0.108

Rate of growth from 1941 and 1951 =  $\frac{15873}{44522}$  = 0.356

Rate of growth from 1951 and 1961 =  $\frac{15219}{60395}$  = 0.252

Rate of growth from 1971 and 1981 =  $\frac{23272}{75614}$  = 0.308

Rate of growth from 1971 and 1981 =  $\frac{25344}{98886}$  = 0.256

1981 and 1971  $= \frac{34570}{124230} = 0.278$ 

Geometric mean,  $r = \sqrt[6]{0.108 \times 0.356 \times 0.252 \times 0.308 \times 0.256 \times 0.278} = 0.244$ 

Assuming that the future growth follow the geometric mean for the period 1921 to 1981

r = 0.244

Population in 2011 = Population in 1981  $\times$  (1 + r)<sup>2</sup>

 $= 158800 \times (1 + 0.244)^2 = 245800$ 

Population in 2016 = Population in 1981  $\times$  (1 + r)<sup>3.5</sup>

 $= 158800 \times (1 + 0.244)^{3.5} = 340980$ 



#### 3. Method of Varying Increment or Incremental Increase Method

In this method a progressively decreasing or increasing rather than a constant rate is adopted. This is a modification over the Arithmetical Progression Method.

Year (Y)	Population	Increase (X)	Incremental Increase
1921	40185	_	_
1931	44522	4337	_
1941	60395	15873	11536
1951	75614	15219	-654
1961	98886	23272	8053
1971	124230	25344	2072
1981	158800	34570	9226
Total		118615	30233

Average = 
$$\frac{118615}{6}$$
 = 19769  

$$Y = \frac{30233}{5} = 6047$$

$$P_n = P_1 + nX + \frac{n(n+1)Y}{2}$$

$$P_{2001} = P_{1981} + 2 \times 19769 + \frac{2 \times 3 \times 6047}{2}$$

$$= 158800 + 39538 + 18141 = 216479$$

$$P_{2016} = P_{1981} + 3.5 \times 19769 + \frac{(3.5 \times 4.5 \times 6047)}{2}$$

$$= 158800 + 69192 + 47620 = 275612$$

In a town, it has been decided to provide 200 litres per head per day in the 21st century. Estimate the domestic water requirements of this town in the year AD 2000 by projecting the population of the town by incremental increase method:

Year	1940	1950	1960	1970	1980
Population	2,37,98,624	4,69,78,325	5,47,86,437	6,34,67,823	6,90,77,421

#### **Solution:**

Thy given population data is analysed, as shown in table below:

Year	Population	Increase in population	Increment over the increase, i.e. incremental increase
(1)	(2)	(3)	(4)
1940	2,3798,624		
1950	4,69,78,325	2,31,79,701	(-) 1,53,71,589
1960	5.4786,437	78,08,112	(+) 8,73,274
1970	6,34,67,823	86,81386	(-) 30,71,788
1980	6,90,77,421	5609,598	
Total		4,52,78,797	(-) 1,75,70,103
Average per decade		x = 1,13,19,699	$\overline{y} = (-)\frac{1,75,70,103}{3}$ = (-) 58,56,701





Expected population at the end of year 2000 (i.e. after 2 decades from 1980)

$$= P_2 = P_0 + 2.\overline{x} + \frac{2 \times 3}{2}.\overline{y}$$
  
= 6,90,77,421 + 2(1, 13,19,699) - 3(58,56,701) = 7,41,46,716

... Water requirement in AD 2,000 @ 200 I/head/d

$$= \frac{200 \times 7,41,46,716}{10^6} Ml/day = 14,829 MLD$$

Q.10 The population of a small town for a 5 decades from 1970 to 2010 is given below. Find the population in the year 2020, 2030 and 2040 by using arithmetic increase method, geometric increase method and incremental increase method.

Year	1970	1980	1990	2000	2010
Population	25000	28000	34000	42000	47000

#### **Solution:**

Given data:

Year	Population	Increase	Increase in increases
1970	25000		
1980	28000	3000	
1990	34000	6000	3000
2000	42000	8000	2000
2010	47000	5000	-3000
		<del>X</del> = 5500	<i>Y</i> = 666.67

#### (i) By arithmetic increase method

- (a) population in 2020 = 47000 + 5500 = 52500
- (b) population in  $2030 = 47000 + 2 \times 5500 = 58000$
- (c) population in  $2040 = 47000 + 3 \times 5500 = 63500$

#### (ii) By incremental increase method

(a) population in 2020 = 47000 + 5500 + 
$$\frac{1 \times 2}{2} \times 666.67 = 53167$$

(b) population in 2030 = 47000 + 2 × 5500 + 
$$\frac{2 \times 3}{2}$$
 × 666.67 = 60000

(c) population in 2040 = 47000 + 3 × 5500 + 
$$\frac{3 \times 4}{2}$$
 × 666.67 = 67500

#### (iii) By geometric increase method

- (a) population in  $2020 = 47000 \times (1 + 0.164) = 54708$
- (b) population in  $2030 = 47000 \times (1 + 0.164)^2 = 63680$
- (c) population in  $2040 = 47000 \times (1 + 0.164)^3 = 74124$

Year	Population	Increase	Growth rate
1970	25000		
1980	28000	3000	0.12
1990	34000	6000	0.214
2000	42000	8000	0.235
2010	47000	5000	0.119
			$\overline{r}$ = 0.164

Q11 The census record of a particular town shows the population figures as follows:

Years	1960	1970	1980	1990
Population	55,500	63,700	71,300	79,500

Estimate the population for the year 2020 by Decreasing Rate of Growth.